

# Improving Security of A Communication-efficient Three-party Password Authentication Key Exchange Protocol

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## Abstract

Three-party Password-based Authentication Key Exchange (3PAKE) allows a trusted server to assist two users to establish a common session key. Recently, Wu et al. pointed out that Chang et al.'s 3PAKE was vulnerable to the off-line guessing attack and proposed an improved 3PAKE to fix the problem. However, we found that Wu et al.'s protocol is still subject to the off-line guessing attack. In addition, the paper offers a simple method to detect the attack.

*Keywords: Authentication, cryptanalysis, guessing attack, key exchange, password-based, three-party*

## 1 Introduction

To verify remote users' identities, password authentication schemes are most commonly used when it comes to allowing users to choose their own passwords [5, 6, 11, 12, 22, 25, 28-30, 33-37, 43]. Lamport [16] was the first to propose a password authentication scheme, and since then password authentication schemes have prospered and developed into many new forms [1, 3, 4, 7-10, 13-15, 26, 27, 31, 32, 39, 42], among which Password-based Authentication Key Exchange (PAKE) is now a main stream.

### 1.1 Related Work

The first password-based authentication key exchange protocol was proposed by Bellare and Merritt [1]. Using their PAKE protocol, two users can share a password to establish their common session key. However, PAKE cannot live up to the requirement of modern multi-user systems, so many researchers [2, 23, 24, 38, 40, 41] have endeavored to develop PAKE into three-party password-based authentication key exchange (3PAKE) protocols. In a 3PAKE design, there is a trusted server that assists two

users to cooperate in establishing a common session key which they can use to communicate with each other privately [17-21].

Among the many 3PAKE protocols, Chang et al.'s work [2], which is based on LHL-3PAKE [24], is quite an outstanding design. Chang et al.'s protocol needs no server's public key and no symmetric cryptosystems, and they claim that the protocol meets such security requirements as mutual authentication, session key security, know-key security, forward secrecy, and protection against the off-line password guessing attack. Unfortunately, Wu et al. [38] pointed out the fact that Chang et al.'s protocol has a flaw against the off-line guessing attack. Wu et al. then proposed an improved protocol to remedy the security weakness.

### 1.2 Contributions

However, we found that Wu et al.'s protocol is still vulnerable to the off-line guessing attack. Therefore, in this paper, we will prove that even Wu et al.'s protocol is not secure enough against the off-line guessing attack. In addition, the paper offers a simple method to detect the attack.

### 1.3 Organization

The organization of this paper is as follows. Section 2 will be a brief review of Wu et al.'s protocol. Then, in Section 3, we will show why Wu et al.'s protocol is still vulnerable to the off-line password guessing attack. In Section 4, we will propose a simple method to detect the attack. Finally, the conclusion will be presented in Section 5.

## 2 Review of Wu et al.'s Protocol

In this Section, we review the three-party password

Table 1: The notations

Notations	Description
$\varepsilon$	An elliptic curve defined over a finite field $GF(p)$
$P$	A base point in $\varepsilon$ with large order $q$ , where $q$ is a secure large prime
$G$	A cyclic additive group generated by $P$
$x \cdot P$	The point multiplication defined as $x \cdot P = P + P + \dots + P(x \text{ times})$
$Z_q$	The ring of integers modulo $q$ , $Z_q = \{0, 1, \dots, q - 1\}$
$Z_q^*$	The multiplicative group of non-zero integers modulo $q$
$\mathcal{H}(\cdot)$	A one-way hash function: $\{0, 1\}^* \rightarrow \{0, 1\}^l$
$\parallel$	A concatenation of bit strings
$A, B$	Two communication clients (users) (also representing their identities)
$S$	The trusted server(also representing its identities)
$PW_A, PW_B$	$A$ 's and $B$ 's password secretly shared with $S$

authenticated key exchange protocol proposed by Wu et al. [38]. In Table 1 below, there are some notations used in Wu et al.'s protocol.

The structure of their protocol is illustrated in Figure 1, and the detailed steps are as follows. To begin with, the expression  $A \rightarrow B: \langle m \rangle$  means  $A$  sends a message  $m$  to  $B$ .

Step 1:  $A \rightarrow S: \langle A, B \rangle$

$A$  sends his/her identity and  $B$ 's identity to the trusted server  $S$  as an initial request.

Step 2:  $S \rightarrow A: \langle Y_A, Y_B \rangle$

After receiving  $A$ 's request,  $S$  chooses two random numbers  $y_A, y_B \in Z_q^*$  and computes  $Y_A = y_A P + PW_A$  and  $Y_B = y_B P + PW_B$ , then sends  $Y_A$  and  $Y_B$  to  $A$ .

Step 3:  $A \rightarrow B: \langle A, X_A, Y_B, \alpha_{AS} \rangle$

When  $A$  receives  $Y_A$  and  $Y_B$  from  $S$ ,  $A$  chooses a random number  $x_A \in Z_q^*$  to compute  $X_A = x_A P$ ,  $K_{AS} = x_A(Y_A - PW_A)$  and the hash value  $\alpha_{AS} = \mathcal{H}(A \parallel S \parallel B \parallel X_A \parallel Y_A \parallel PW_A \parallel K_{AS})$ . After computing these values,  $A$  sends  $\langle A, X_A, Y_B, \alpha_{AS} \rangle$  to  $B$ .

Step 4:  $B \rightarrow S: \langle X_A, X_B, Y_B, \alpha_{AS}, \alpha_{BS} \rangle$

After  $B$  receives  $A$ 's messages,  $B$  chooses a random number  $x_B \in Z_q^*$  to compute  $X_B = x_B P$ ,  $K_{BS} = x_B(Y_B - PW_B)$ ,  $K_{AB} = x_B X_A$ , and two hash values  $\alpha_{BS} = \mathcal{H}(B \parallel S \parallel A \parallel X_B \parallel Y_B \parallel PW_B \parallel K_{BS})$  and  $\gamma_B = \mathcal{H}("1" \parallel A \parallel S \parallel B \parallel X_A \parallel X_B \parallel K_{AB})$ . After computing these values,  $B$  sends  $\langle X_A, X_B, Y_B, \alpha_{AS}, \alpha_{BS} \rangle$  to the server  $S$ .

Step 5:  $S \rightarrow A: \langle X_B, \beta_{AS}, \beta_{BS}, \gamma_B \rangle$

After  $S$  receives  $B$ 's messages,  $S$  uses the number chosen in Step 2 to compute  $K_{AS} = y_A X_A$  and the hash values  $\alpha'_{AS} = \mathcal{H}(A \parallel S \parallel B \parallel X_A \parallel Y_A \parallel PW_A \parallel K_{AS})$ , and then  $S$  verifies the consistency between the computed  $\alpha'_{AS}$  and the value  $\alpha_{AS}$  sent from  $B$ . In order to authenticate  $B$ ,  $S$  computes  $K_{BS} = y_B X_B$  and the hash value  $\alpha'_{BS} = \mathcal{H}(B \parallel S \parallel A \parallel X_B \parallel Y_B \parallel PW_B \parallel K_{BS})$ , and then  $S$  verifies the consistency between the computed  $\alpha'_{BS}$  and the value  $\alpha_{BS}$  sent from  $B$ . If these values are correct,  $S$  computes the

hash values  $\beta_{AS} = \mathcal{H}(A \parallel S \parallel B \parallel X_A \parallel Y_A \parallel PW_A \parallel K_{AS} \parallel X_B)$  and  $\beta_{BS} = \mathcal{H}(B \parallel S \parallel A \parallel X_B \parallel Y_B \parallel PW_B \parallel K_{BS} \parallel X_A)$ , and then  $S$  sends  $X_B, \beta_{AS}, \beta_{BS}, \gamma_B$  to  $A$ .

Step 6:  $A \rightarrow B: \langle \beta_{BS}, \gamma_A \rangle$

When  $A$  receives  $S$ 's messages,  $A$  uses  $K_{AS}$ , which was computed in Step 3, and  $X_B$  to compute the hash value  $\beta'_{AS} = \mathcal{H}(A \parallel S \parallel B \parallel X_A \parallel Y_A \parallel PW_A \parallel K_{AS} \parallel X_B)$ . In order to authenticate  $S$ ,  $A$  verifies the consistency between the computed  $\beta'_{AS}$  and the value  $\beta_{AS}$  sent from  $S$ . If the result is correct,  $A$  computes  $K_{AB} = x_A X_B$  and the hash value  $\mathcal{H}("1" \parallel A \parallel S \parallel B \parallel X_A \parallel X_B \parallel K_{AB})$  and then verifies the value  $\gamma_B$ . If these values are correct,  $A$  can make sure that  $B$  has the ability to compute the session key  $SK = \mathcal{H}(2 \parallel A \parallel S \parallel B \parallel X_A \parallel X_B \parallel K_{AB})$ . After that,  $A$  sends  $\beta_{BS}$  and  $\gamma_A$  to  $B$ .

Step 7:

After receiving  $A$ 's messages,  $B$  derives the hash value  $\mathcal{H}(B \parallel S \parallel A \parallel X_B \parallel Y_B \parallel PW_B \parallel K_{BS} \parallel X_A)$  from  $X_A$  and  $K_{BS}$ . In order to authenticate  $S$ ,  $B$  verifies the consistency between  $\beta_{BS}$  and the hash value  $\mathcal{H}(B \parallel S \parallel A \parallel X_B \parallel Y_B \parallel PW_B \parallel K_{BS} \parallel X_A)$ . If the result is correct,  $B$  computes the hash value  $\mathcal{H}("0" \parallel A \parallel S \parallel B \parallel X_A \parallel X_B \parallel K_{AB})$  and verifies whether the value  $\gamma_A$  which was sent from  $A$  is correct or not. If the result is positive,  $B$  can make sure that  $A$  has ability to compute the session key  $SK = \mathcal{H}(2 \parallel A \parallel S \parallel B \parallel X_A \parallel X_B \parallel K_{AB})$ .

With the above steps done,  $A$  and  $B$  can generate a common session key  $SK = \mathcal{H}(2 \parallel A \parallel S \parallel B \parallel X_A \parallel X_B \parallel K_{AB})$  via the trusted server  $S$ .

### 3 Some vulnerabilities of Wu et al.'s protocol

In this section, we will show that an off-line guessing attack can break Wu et al.'s protocol. An attacker can pretend to be the server and intercept the messages sent from the users. The structures of the steps of our attack are shown in Figure 2, Figure 3, and Figure 4.

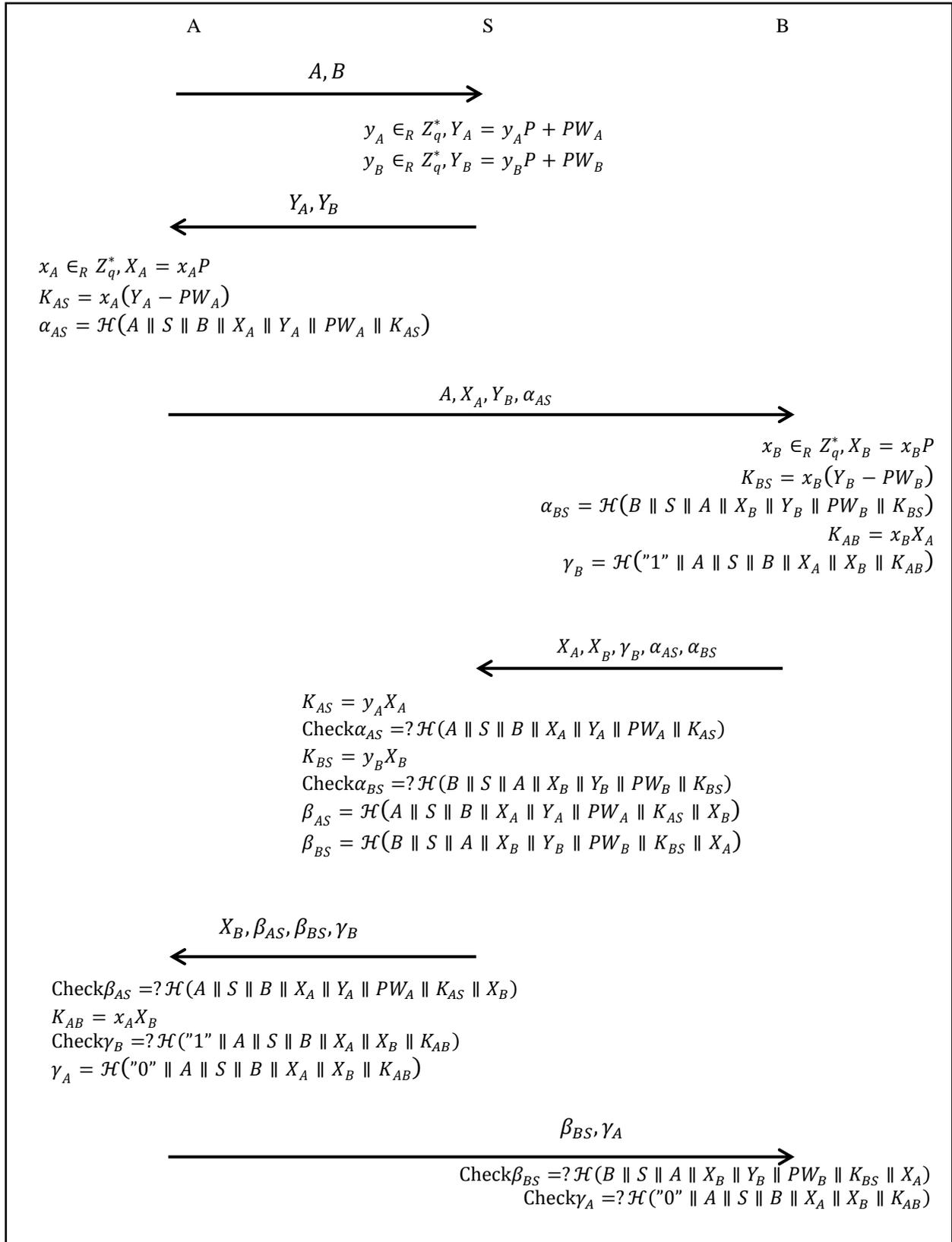


Figure 1: Wu et al.'s 3PAKE protocol

Step 1:

Suppose there is a user  $A$  who wants to communicate with another person  $\star$ .  $A$  sends his/her identity along

with  $\star$ 's identity to the server as an initial request. At this point of time, the attacker  $S^*$  pretends to be the sever  $S$  and intercepts the messages sent from  $A$  and

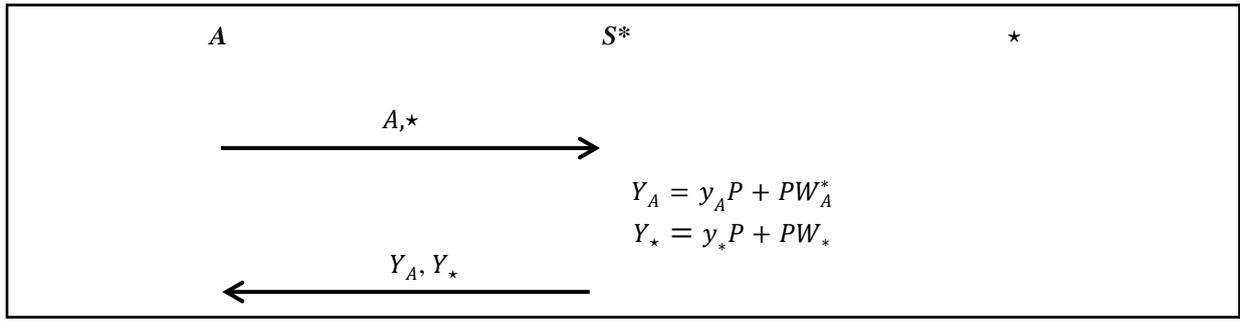


Figure 2: Step 1 of our attack

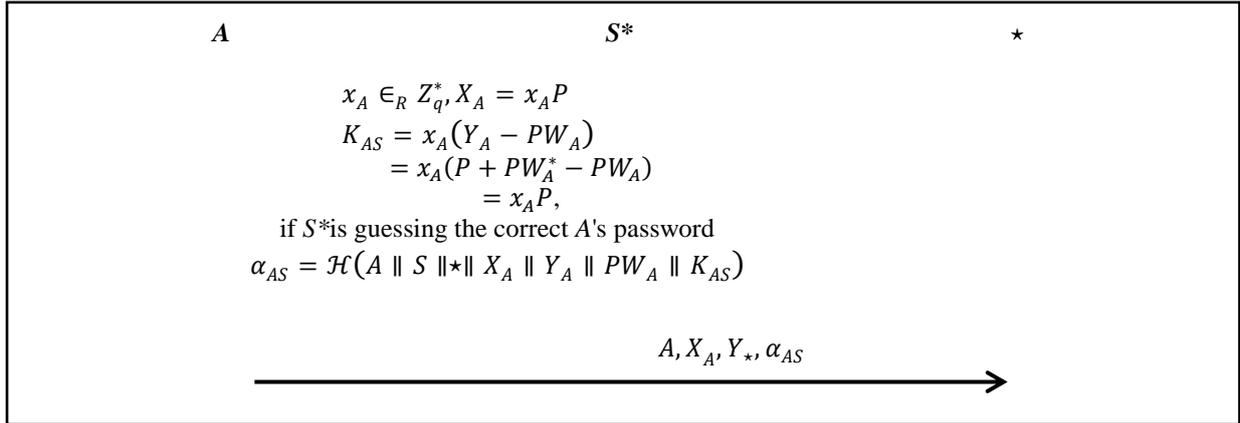


Figure 3: Step 2 of our attack

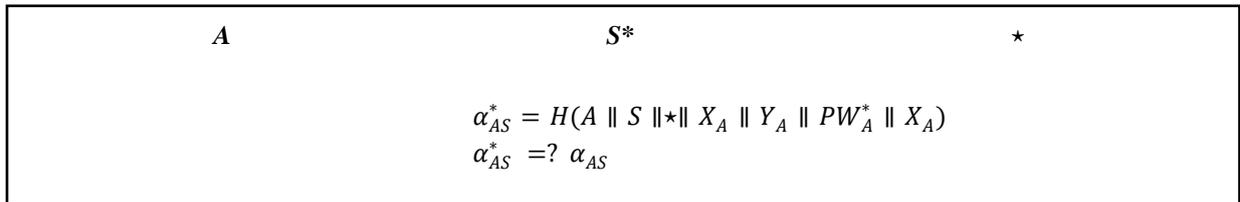


Figure 4: Step 3 of our attack

sets  $y_A=1$  and computes  $Y_A = y_A P + PW_A^*$ , where  $PW_A^*$  is the password which the attacker has guessed. After that,  $S^*$  sends  $Y_A$  and  $Y_*$  to  $A$ , where  $Y_* = y_* P + PW_*$ .  $y_*$  is a random number and  $PW_*$  is a possible password.

Step 2:

When  $A$  receives  $Y_A$  and  $Y_*$  from  $S^*$ ,  $A$  computes  $X_A = x_A P$ ,  $K_{AS} = x_A (Y_A - PW_A)$  and  $\alpha_{AS} = \mathcal{H}(A || S || * || X_A || Y_A || PW_A || K_{AS})$ . After finishing the computation,  $A$  will send  $A, X_A, Y_*, \alpha_{AS}$  to  $*$ . Note that  $\mathcal{H}()$  is a public one-way hash function.

Step 3:

When  $A$  sends  $A, X_A, Y_*, \alpha_{AS}$  to  $*$ , the attacker can intercept the messages and then compute  $\alpha_{AS}^* = \mathcal{H}(A || S || * || X_A || Y_A || PW_A^* || X_A)$ . If the attacker's guess of the password  $PW_A^*$  is correct, then  $K_{AS}$  is equal to  $x_A P$ . The attacker can then use it to compute  $\alpha_{AS}^*$  and check if  $\alpha_{AS}^*$  is equal to  $\alpha_{AS}$ . If it is, the attacker can make sure that he/she has guessed  $A$ 's password.

#### 4 Improving security of Wu et al.' protocol

To detect the attack during the communication, in Step 3 of Wu et al.'s protocol,  $A$  can check to see if  $X_A$  is the same as  $K_{AS}$ . If it holds,  $A$  can be sure that the communication is under attack. In addition, in Step 2 of Wu et al.'s protocol, the server must choose  $y_A$  and  $y_B$  such that  $y_A$  not equal to 1 and  $y_B$  not equal to 1.

#### 5 Conclusions

In this paper, we have shown that Wu et al.'s 3PAKE protocol is still vulnerable to the off-line password guessing attack. In addition, we have also offered a simple method to detect the attack.

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